# OBJECTIVE INDEX FOR THE RADIAL DISTRIBUTION OF LOW-ORDER LATERAL TREE ROOTS 

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#### Abstract

An objective index describing the radial "evenness" of lateral tree roots has been developed. The index may be applied on the basis of root length or mass or image analysis of root quantity. Unevenness, defined as deviation from a perfectly uniform root distribution, is weighted according to the scale at which it occurs, with unevenness between halves or quarters of the root system receiving more weight than unevenness between sixteenths or thirty-seconds. A sliding frame of reference eliminates the problem of rotational dependence in the initial positioning of the "grid" used to count roots. For practical application the index requires a computer-readable root map, either from a field root-mapping exercise, or from digitised pictures of the exposed root system. Agreement between evenness rankings from visual inspection and from the index is generally excellent.


Keywords: root distribution; morphology; tree architecture.

## INTRODUCTION

The evenness of the radial distribution of low-order lateral tree roots is an important characteristic of root system morphology. Plantation trees transplanted as seedlings often have significant unevenness induced by planting technique. This unevenness may make trees more susceptible to windthrow (Bell 1978; Mason 1985), and may be associated with less-efficient use of soil resources. Distortion of the tap root, which may also occur during transplanting, may produce "butt sweep", a bending of the lower part of the tree that reduces its value when felled. To evaluate and compare planting procedures, a measure of root system distortion is required. Several such indices have been reported (Balneaves \& De La Mare 1989; Mason 1985) but these are generally subjective, and also tend to be dependent on the rotation of the frame of reference adopted for the measurement. This subjectivity does not mean that these indices are not useful for assessment within an experimental programme where relative values are more important than absolute values, but it does limit their usefulness for more wide-ranging comparisons.

Objective comparisons of root system morphologies are also important for the calibration and validation of computer models of plant root architecture. Difficulties encountered in the validation of such highly stochastic and irregular structures (Brown \& Kulasiri 1996) prompted the development of the index described here. The index is well suited to situations where both field observations and simulated root architectures are available in the same computer-readable form (Henderson et al. 1983; Brown \& Kulasiri 1994).

## FORMULATION

As with most radial evenness indices, the root system is divided into segments. The root system is considered to be "evenly" distributed when each segment contains the same amount of some measure of root quantity, perhaps length or root mass. For example, if $L \mathrm{~m}$ is the total root length of a root system divided into $N$ segments, each segment should contain $L / N \mathrm{~m}$ of root if the system is distributed evenly. Radial evenness indices intended for application by people in the field commonly use only four or eight segments, typically aligned to a specific compass direction, or to the row of trees being sampled. The low number of segments and arbitrary alignment mean that the same root system can score different evenness values depending on the rotation of the frame dividing it into segments (Fig. 1).


FIG. 1-The same tree could be scored as $1 / 1 / 1 / 1$ or $2 / 0 / 2 / 0$, depending on frame orientation.
The index presented here avoids any dependence on the rotation of the segments by considering all possible halves, quarters, eighths, and so on by dividing the root system into a high number of segments, say 64 , and examining, for example, all 64 sets of 16 contiguous segments which constitute a quarter of the root system. This approach is illustrated in Fig 2, where only eight segments are used for clarity.


The index is the weighted sum of deviation from the expected $1 / 8$ of total in eight segments $A, B, C, D, \ldots H$, plus deviation from $1 / 4$ of total in eight overlapping "quarters" $\mathrm{AB}, \mathrm{BC}, \mathrm{CD}, \mathrm{DE}, \ldots \mathrm{HA}$, plus deviation from $1 / 2$ of total eight overlapping "halves" $\mathrm{ABCD}, \mathrm{BCDE}, \mathrm{CDEF}, \ldots$ HABC. Finally, the index is divided by the maximum possible value of the above summation, which for eight segments is 70 .

FIG. 2-Overlapping alignment.

The index is the weighted sum of deviations at each scale, from ${ }^{1 / 2}$ down to $1 / N$, where $N$ is the number of segments used. In general $N$ will be a power of 2 . If segments are labelled $1 \ldots N$, and $O_{i}$ denotes the proportion of total root length (or mass, etc.) observed in segment $i$, then the value of the index is increased by $\left|O_{i}-1 / N\right|$ for each segment (where $1 / N$ is the proportion expected in each segment of an even system and $|x|$ denotes the absolute value of $x$ ). Simlarly, every two contiguous segments should contain $2 / N^{\text {ths }}$ of the root system. As the scale increases from $1 / N$ up to $1 / 2$ of the root system, deviation from the expected fraction of total root length becomes more significant, in terms of its impact on tree stability and root evenness. But the number of segments comprising successively larger fractions of the root system also increases, thereby weighting deviations from even distribution at larger scales more heavily.

If a value $c$ is defined such that $c=\log _{2} N$ (i.e., $2^{c}=N$ ), the index is the total of three layers of summation, each of $c$ levels of scale contains $2^{c}$ (or $N$ ) sets of $2^{c}-i$ segments, where $i$ is the scale level from 1 (half the root system) to $c$ (one segment). The index should be divided by its maximum value, $M$, to give a value ranging from 0 (perfectly even distribution) to 1 (all roots in one segment). The first author can be contacted for source code or assistance with implementation of the index. The complete index is given in Equation 1.

$$
\begin{equation*}
\text { Index }=\sum_{i=1}^{c} \sum_{j=1}^{2^{c}}\left|\sum_{k=1}^{2^{c-i}} O_{j+k-1}-\frac{1}{2^{i}}\right| \times M^{-1} \tag{1}
\end{equation*}
$$

where $Q_{x}=$ the proportion of root mass or length occurring in segment $x$ if $x>2^{c}$, subtract $2^{c}$ from $x$
$M=$ the maximum of the summation (all roots in one segment). $\sum_{i=1}^{c}\left(2^{c+1-i}-2^{c+1-2 i}\right)$

## EXAMPLES

Given the system pictured, with 10 roots of equal length, the index is calculated as follows (note that eight segments are too few to avoid the influence of rotation described abovein reality, 64 is probably an ideal number):


| Segment | Root length | $O_{i}$ |
| :---: | :---: | :---: |
| 1 | 2 | 0.2 |
| 2 | 0 | 0.0 |
| 3 | 1 | 0.1 |
| 4 | 0 | 0.0 |
| 5 | 0 | 0.0 |
| 6 | 5 | 0.5 |
| 7 | 2 | 0.2 |
| 8 | 0 | 0.0 |

$$
A=\left|\sum_{k=1}^{2^{c-i}} O_{j+k-1}-\frac{1}{2^{i}}\right|
$$

| j | Halves$i=1$ |  | Quarters $i=2$ |  | $\begin{gathered} \text { Segments } \\ i=3 \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | k | $A$ | k | $A$ | k | $A$ |
| 1 | 1,2,3,4 | 0.200 | 1,2 | 0.050 | 1 | 0.075 |
| 2 | 2,3,4,5 | 0.400 | 2,3 | 0.150 | 2 | 0.125 |
| 3 | 3,4,5,6 | 0.100 | 3,4 | 0.150 | 3 | 0.025 |
| 4 | 4,5,6,7 | 0.200 | 4,5 | 0.250 | 4 | 0.125 |
| 5 | 5,6,7,8 | 0.200 | 5,6 | 0.250 | 5 | 0.125 |
| 6 | 6,7,8,1 | 0.400 | 6,7 | 0.450 | 6 | 0.375 |
| 7 | 7,8,1,2 | 0.100 | 7,8 | 0.050 | 7 | 0.075 |
| 8 | 8,1,2,3 | 0.200 | 8,1 | 0.050 | 8 | 0.125 |
|  |  | 1.8 |  | 1.4 |  | 1.05 t |

Normalised evenness index (divide by $M$ ) $4.25 / 8.75=0.486$. The boxed 0.200 value occurs because the half represented by segments $1-4$ should contain $0.5(4 / 8)$ of the total root system, but in fact contains only 0.3 . Similarly, the boxed 0.375 occurs because segment 6 should contain only $0.125(1 / 8)$ of the total root system, but in fact contains $0.5(5 / 10), 0.375$ $=0.5-0.125$.

Some other possible arrangements and their scores are illustrated in Fig. 3 for comparison. The failure to distinguish between the two examples which score 0.51 in Fig. 3 is a side effect

0.11

0.51


FIG. 3-Examples of (un)evenness index scores.
of using only eight segments; the index is intended for computerised application to precise root maps or image data, where a larger number of segments would be used. Index values for root maps derived from data (Table 1) generously made available by Alex Watson (Watson \& O'Loughlin 1990) are given in Fig. 4. Note that the index measures distribution around the centre of the root system, i.e., the base of the stem, and so a root collar off-centre in an otherwise relatively even root system will score highly. Where shown, grids are $1 \times 1 \mathrm{~m}$ spacing.

## DISCUSSION

The index may require some fine tuning for specific applications, although its general form is probably sufficient for most uses. Roots of different orders could be weighted to differing degrees, or examined separately, if the root map being used was sufficiently sophisticated and the behaviour of different orders warranted the distinction. Root number is probably not the ideal measure of root quantity, as one root may curve and pass through many segments, particularly when the segments are narrow as happens when a high number of segments are used.

Digitised images of root systems may also be used as computer-readable input for the index. After the stem has been removed, careful excavation will allow a root system to be exposed in situ without displacement. A photograph or video recording of the exposed system taken from directly above the root collar may be digitised (Brown 1994). Minor image processing can produce a binary (two-colour) image of the root system against a blank background. The roots may be spray-painted with fluorescent paint to increase contrast if necessary. Given the location of the centre of the root system within the image, a simple pixel to segment mapping can be used to provide an index of the amount of "material" in each segment the $O_{i}$ input to the index.

## CONCLUSION

As it is often not feasible to find a simple set of practical measurements which adequately define complex, variable, biological entities such as root systems, indirect comparisons with their real-world counterparts may be useful. The index presented here ranks root systems according to "evenness", a very widely applicable characteristic often used subjectively for both identification and comparison. The index's specification in a form suitable for objective repeatable use with computer-readable root maps allows it to be used for inter-trial comparisons, and for model calibration applications.

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TABLE 1-Data (image pixel counts) for trees in Fig. 4. In that Figure the trees are ordered 3, 4, 5, 2, 1 and 2, 1, 5, 4, 3 for 8 - and 16-year groups respectively.

| Eight-year-old trees |  |  |  |  |  |  |  |  |  | Sixteen-year-old trees |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | 2 |  | 3 |  | 4 |  | 5 |  | 1 |  | 2 |  | 3 |  | 4 |  | 5 |  |
| 642 | 656 | 204 | 213 | 246 | 257 | 261 | 395 | 541 | 312 | 611 | 381 | 931 | 1200 | 77 | 72 | 204 | 51 | 143 | 224 |
| 2170 | 1137 | 709 | 776 | 162 | 146 | 105 | 228 | 747 | 758 | 638 | 1207 | 1257 | 1180 | 69 | 203 | 29 | 559 | 239 | 405 |
| 869 | 718 | 403 | 327 | 245 | 341 | 221 | 613 | 66 | 73 | 1132 | 1241 | 1130 | 995 | 193 | 400 | 816 | 1113 | 303 | 193 |
| 344 | 302 | 199 | 117 | 228 | 246 | 713 | 395 | 189 | 109 | 1216 | 1444 | 1176 | 1060 | 784 | 1079 | 698 | 1168 | 184 | 301 |
| 271 | 163 | 125 | 97 | 387 | 643 | 145 | 243 | 167 | 496 | 1746 | 2423 | 371 | 1632 | 1077 | 1613 | 845 | 428 | 618 | 1137 |
| 78 | 8 | 85 | 80 | 519 | 212 | 256 | 1088 | 200 | 388 | 1296 | 1092 | 973 | 521 | 986 | 1299 | 279 | 360 | 946 | 926 |
| 8 | 12 | 78 | 82 | 217 | 149 | 806 | 773 | 371 | 904 | 1194 | 1790 | 1746 | 779 | 1742 | 1385 | 241 | 665 | 801 | 356 |
| 18 | 21 | 97 | 104 | 147 | 152 | 943 | 739 | 1166 | 717 | 943 | 549 | 683 | 797 | 1176 | 537 | 666 | 1101 | 464 | 342 |
| 12 | 20 | 132 | 269 | 106 | 120 | 1466 | 885 | 365 | 923 | 582 | 578 | 1177 | 865 | 496 | 479 | 1056 | 551 | 176 | 301 |
| 18 | 22 | 296 | 291 | 111 | 175 | 370 | 254 | 379 | 394 | 1631 | 1509 | 704 | 570 | 574 | 388 | 1362 | 680 | 381 | 396 |
| 26 | 29 | 367 | 322 | 256 | 487 | 210 | 121 | 464 | 574 | 863 | 925 | 1267 | 944 | 478 | 1109 | 753 | 448 | 303 | 260 |
| 33 | 188 | 234 | 111 | 178 | 230 | 98 | 51 | 732 | 220 | 624 | 660 | 1226 | 757 | 1927 | 1039 | 657 | 749 | 527 | 465 |
| 207 | 140 | 311 | 104 | 303 | 323 | 41 | 351 | 109 | 111 | 739 | 888 | 652 | 497 | 612 | 421 | 1008 | 1090 | 422 | 838 |
| 111 | 88 | 134 | 101 | 216 | 227 | 683 | 322 | 79 | 48 | 689 | 828 | 519 | 404 | 784 | 1539 | 1299 | 1594 | 1623 | 884 |
| 221 | 308 | 278 | 318 | 269 | 1130 | 678 | 2175 | 63 | 83 | 625 | 472 | 459 | 535 | 1107 | 354 | 1033 | 405 | 1031 | 1019 |
| 324 | 740 | 378 | 503 | 842 | 771 | 730 | 1227 | 101 | 143 | 289 | 342 | 530 | 851 | 1199 | 481 | 636 | 736 | 578 | 487 |
| 696 | 601 | 442 | 316 | 557 | 932 | 739 | 214 | 142 | 144 | 387 | 251 | 1140 | 1011 | 303 | 331 | 1351 | 1096 | 561 | 543 |
| 1281 | 330 | 381 | 112 | 292 | 284 | 109 | 290 | 122 | 214 | 626 | 1155 | 815 | 816 | 335 | 361 | 952 | 398 | 645 | 739 |
| 400 | 227 | 141 | 261 | 587 | 359 | 177 | 218 | 717 | 435 | 724 | 527 | 1208 | 904 | 504 | 474 | 404 | 177 | 637 | 609 |
| 538 | 262 | 173 | 272 | 284 | 302 | 404 | 356 | 459 | 567 | 1104 | 878 | 1694 | 433 | 331 | 643 | 11 | 13 | 845 | 1102 |
| 94 | 77 | 326 | 330 | 376 | 602 | 394 | 235 | 789 | 1054 | 388 | 316 | 845 | 1284 | 309 | 230 | 188 | 394 | 1028 | 743 |
| 151 | 472 | 122 | 125 | 401 | 843 | 190 | 173 | 960 | 531 | 466 | 501 | 1100 | 556 | 231 | 230 | 1151 | 1479 | 1121 | 1376 |
| 610 | 297 | 29 | 25 | 480 | 234 | 299 | 365 | 726 | 736 | 182 | 155 | 1093 | 1231 | 449 | 589 | 806 | 1175 | 1007 | 556 |
| 198 | 274 | 20 | 94 | 94 | 67 | 596 | 1252 | 943 | 1037 | 811 | 912 | 1022 | 506 | 914 | 837 | 1771 | 884 | 464 | 412 |
| 538 | 256 | 307 | 313 | 80 | 103 | 586 | 306 | 1056 | 1278 | 1222 | 2402 | 258 | 477 | 405 | 431 | 305 | 231 | 444 | 1125 |
| 460 | 221 | 275 | 376 | 564 | 443 | 320 | 233 | 911 | 640 | 2326 | 987 | 469 | 337 | 1161 | 693 | 162 | 293 | 1466 | 1339 |
| 255 | 695 | 513 | 453 | 754 | 657 | 187 | 127 | 505 | 521 | 806 | 1183 | 321 | 479 | 550 | 951 | 178 | 68 | 795 | 1092 |
| 923 | 1400 | 399 | 449 | 336 | 99 | 76 | 73 | 267 | 148 | 742 | 1324 | 758 | 786 | 229 | 166 | 184 | 229 | 837 | 1040 |
| 1106 | 966 | 266 | 519 | 76 | 126 | 55 | 168 | 110 | 236 | 874 | 834 | 1951 | 1828 | 105 | 230 | 272 | 628 | 1087 | 1102 |
| 1025 | 1489 | 849 | 827 | 235 | 245 | 229 | 367 | 172 | 162 | 1192 | 1044 | 585 | 1461 | 291 | 242 | 428 | 397 | 932 | 562 |
| 1143 | 946 | 299 | 806 | 298 | 609 | 501 | 403 | 99 | 93 | 893 | 657 | 1852 | 1544 | 195 | 99 | 321 | 607 | 851 | 558 |
| 432 | 631 | 1000 | 249 | 438 | 574 | 359 | 432 | 113 | 209 | 420 | 414 | 2012 | 4125 | 90 | 76 | 319 | 245 | 1104 | 218 |

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FIG. 4-Index values (64 segments) for 8 - and 16 -year-old Pinus radiata D.Don.

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